

# Introduction to Massive MIMO

## *Communication system concepts*

Dr. Emil Björnson

Associate Professor

Department of Electrical Engineering (ISY)

Linköping University, Sweden



# Outline

- Introduction
- How to Achieve Higher Spectral Efficiency
- Basic Properties of Massive MIMO
- Massive MIMO Transmission Protocol
- Summary

# INTRODUCTION

# Incredible Success of Wireless Communications

## ***Martin Cooper's law***

*The number of voice/data connections has doubled every 2.5 years (+32% per year) since the beginning of wireless*

Last 45 years: 1 Million increase in wireless traffic

*Two-way radio, FM radio, satellites, cellular, WiFi, etc.*

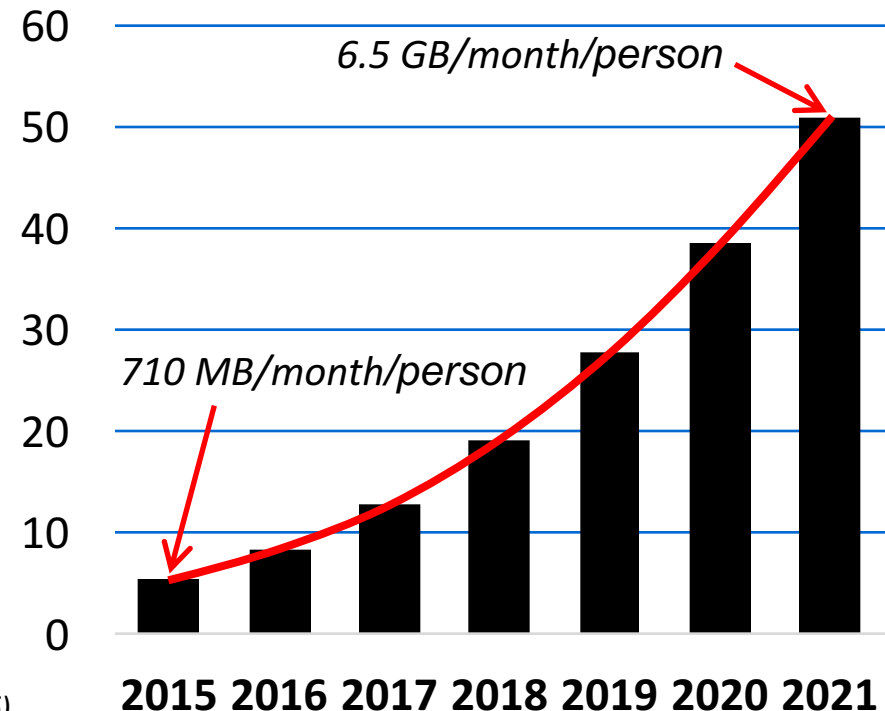


Source: Wikipedia

- **Future Network Traffic Growth**

- 45% annual data traffic growth
- Slightly faster than in the past!
- Exponential increase
- Extrapolation: 6x in 5 years  
40x in 10 years  
260x in 15 years

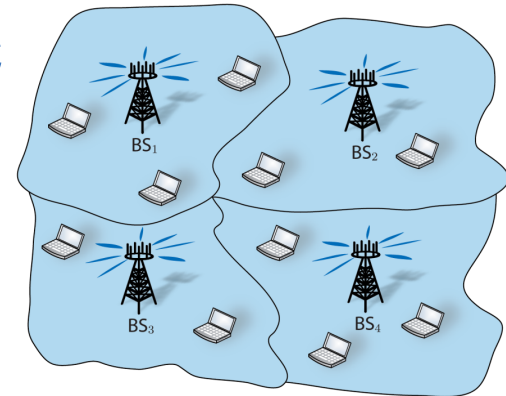
Exabyte/month



# Evolving Networks for Higher Traffic

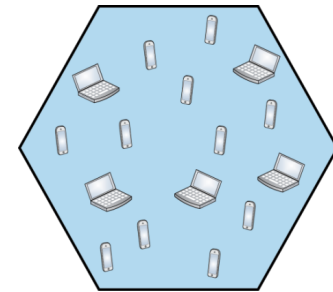
## ***Cellular networks***

Coverage area divided into cells  
Users served by a base station



- Increase Network Throughput [bit/s/km<sup>2</sup>]

- Consider a given area →



- Simple Formula for Network Throughput:

$$\underbrace{\text{Throughput}}_{\text{bit/s/km}^2} = \underbrace{\text{Cell density}}_{\text{Cell/km}^2} \cdot \underbrace{\text{Available spectrum}}_{\text{Hz}} \cdot \underbrace{\text{Spectral efficiency}}_{\text{bit/s/Hz/Cell}}$$

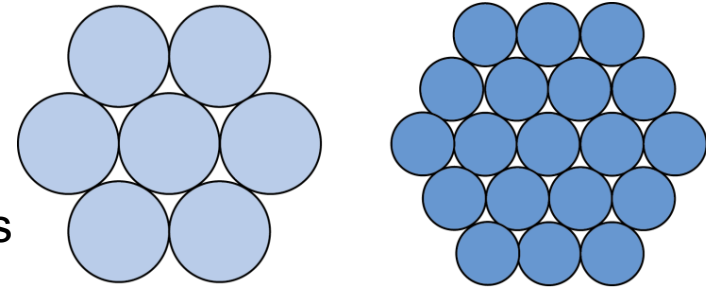
- Ways to achieve 1000x improvement:

	Higher cell density	More spectrum	Higher spectral efficiency
Nokia (2011)	10x	10x	10x
SK Telecom (2012)	56x	3x	6x

# Conventional Solutions

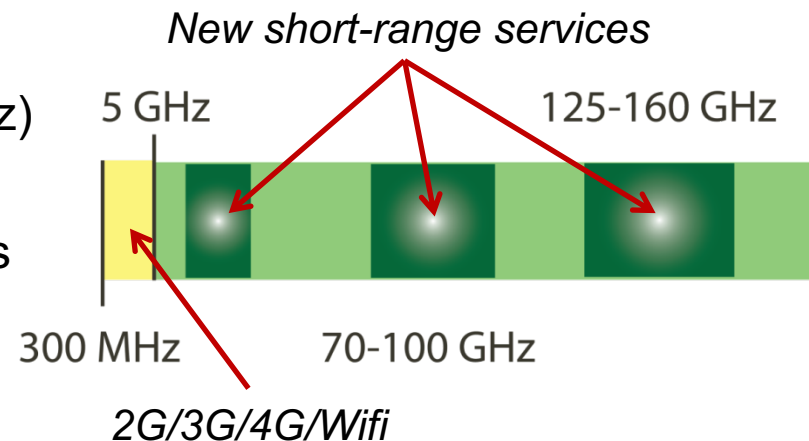
- Higher Cell Density

- Traditional way to improve throughput
- Cut cell radius by  $z \rightarrow z^2$  times more cells
- Issues: High rent and deployment costs  
Interference is getting worse  
WiFi + Cellular is already dense: *Coverage is the issue!*



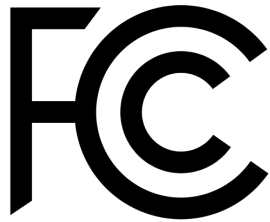
- More Spectrum

- Range suitable for coverage:  $< 5$  GHz
- Already allocated for services!  
(Cellular:  $\sim 550$  MHz, WiFi:  $\sim 550$  MHz)
- Far above 5 GHz: High propagation losses  $\rightarrow$  Mainly short-range hotspots



# Higher Spectral Efficiency

*“Imagine that we decided to reward the first person who finds a way to make spectrum use below 5 GHz 50 or 100 times more efficient over the next decade. The reward could be something simple—say 10 megahertz of spectrum suitable for mobile broadband.”*



**FCC Commissioner Jessica Rosenworcel**  
Marconi Society Anniversary Symposium, Oct. 2, 2014.

## ***Price of sub-5 GHz Spectrum***

*January 2015: FCC sold 65 MHz at 1.7-2.1 GHz for \$45 billion*

**Can FCC's 50× goal be reached?**

How to achieve

**HIGHER SPECTRAL EFFICIENCY**



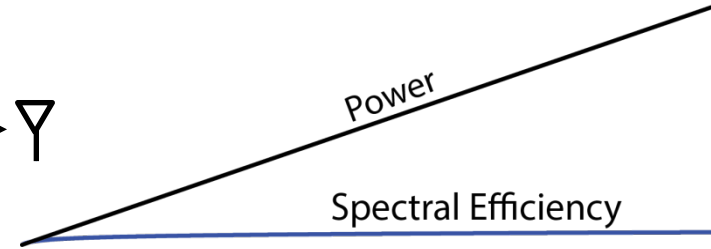
# Higher Spectral Efficiency

- Point-to-Point Spectral Efficiency:  $\nabla \rightarrow \nabla$

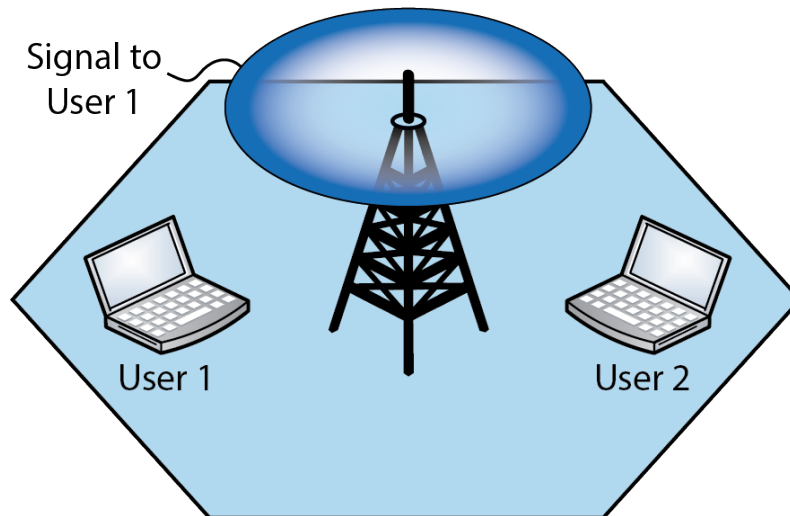
- Governed by Shannon's capacity limit:

$$\log_2 \left( 1 + \frac{\text{Received Signal Power}}{\text{Interference Power} + \text{Noise Power}} \right) \text{ [bit/s/Hz/user]}$$

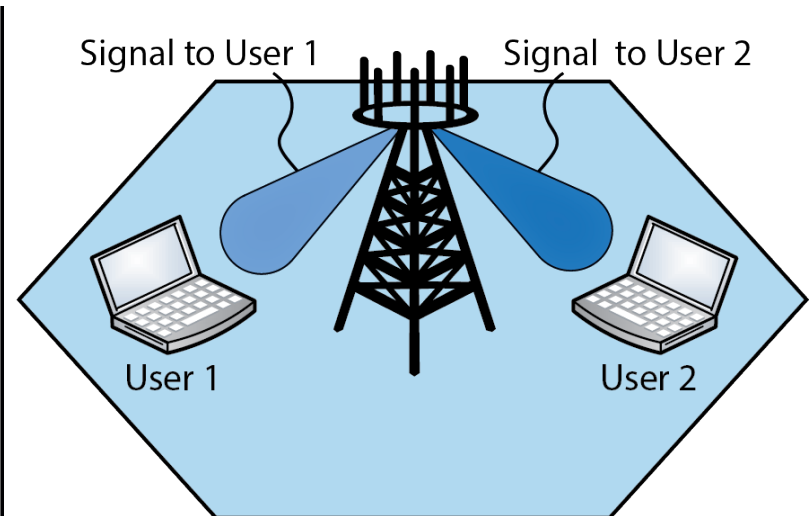
- Issue: 4 bit/s/Hz  $\rightarrow$  8 bit/s/Hz requires 17 $\times$  more power!



- Many Parallel Transmissions: *Spatially focused to each desired user*



Single-Antenna Transmission



Multi-Antenna Transmission

# Multi-User MIMO (Multiple-input Multiple-output)

- Cellular Multi-User MIMO
  - Base stations (BSs) with  $M$  antennas
  - Parallel uplink/downlink for  $K$  users
  - Channel coherence block:  $\tau_c$  symbols

- Theory: Hardware is Limiting

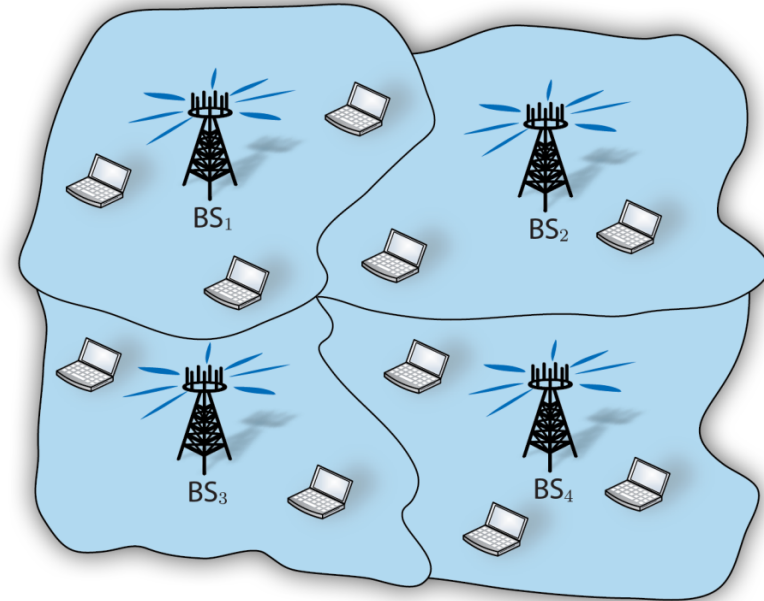
- Spectral efficiency roughly prop. to

$$\min\left(M, K, \frac{\tau_c}{2}\right)$$

- $2\times$  improvement =  $2\times$  antennas and users  $(\tau_c \in [100, 10000])$

- Practice: Co-User Interference is Limiting

- Multi-user MIMO in LTE-A: Up to 8 antennas
  - Small gains: Hard to learn users' channels  
Hard to coordinate BSs



**End of the MIMO road?**

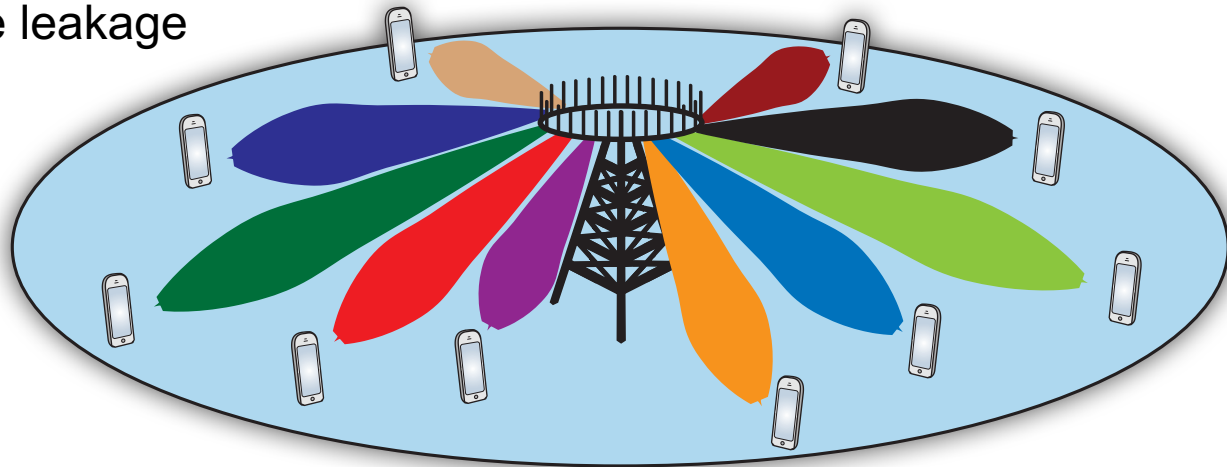
*No reason to add  
more antennas/users?*

# Taking Multi-User MIMO to the Next Level

- Network Architecture: Massive MIMO
  - Many BS antennas; e.g.,  $M \approx 200$  antennas,  $K \approx 40$  single-antenna users
  - Key: Many more antennas than users:  $M \gg K$
  - Very directive signals
  - Little interference leakage

*Spectral efficiency prop.  
to number of users!*

$$\min\left(M, K, \frac{\tau_c}{2}\right) \approx K$$



- Seminal work:
  - T. Marzetta, “Noncooperative Cellular Wireless with Unlimited Numbers of Base Station Antennas,” IEEE Trans. Wireless Communications, 2010.
- 2013 IEEE Guglielmo Marconi Prize Paper Award
- 2015 IEEE W. R. G. Baker Award

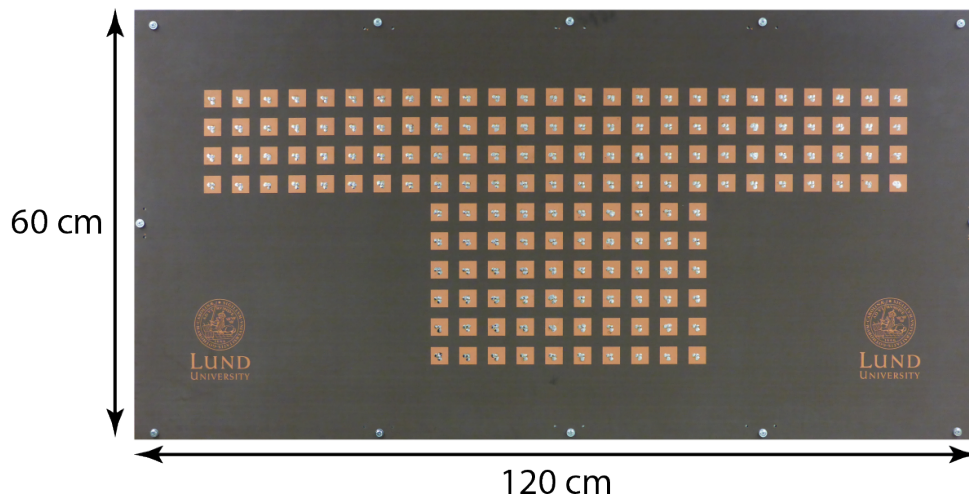
# What is the Key Difference from Today?

- Number of Antennas? **No, we already have many antennas!**
  - 3G/UMTS: 3 sectors x 20 element-arrays = 60 antennas
  - 4G/LTE-A: 8-MIMO x 30 = 240 antennas

## Massive MIMO Characteristics

*Many fully digital steerable antennas*

*Massive in numbers – not massive in size*



**160 antenna elements, LuMaMi testbed, Lund University**

*Typical vertical array:  
10 antennas x 2 polarizations  
Only 2 antenna ports*



**3 sectors, 4 vertical arrays per sector**

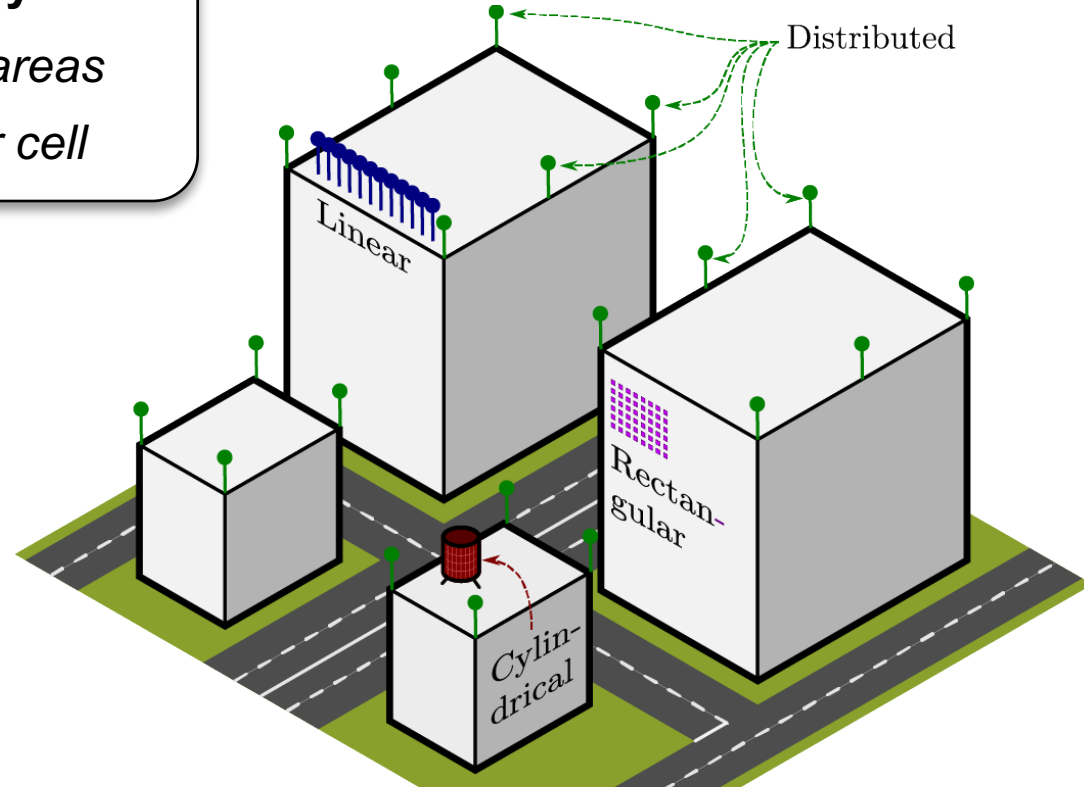
# How to Deploy Massive MIMO?

## Conventional Cellular Deployment

*Non-overlapping coverage areas*

*One or multiple sectors per cell*

- Co-located Deployment
  - 1D, 2D, or 3D arrays
  - No need for sectors
- Distributed Deployment
  - Remote radio heads

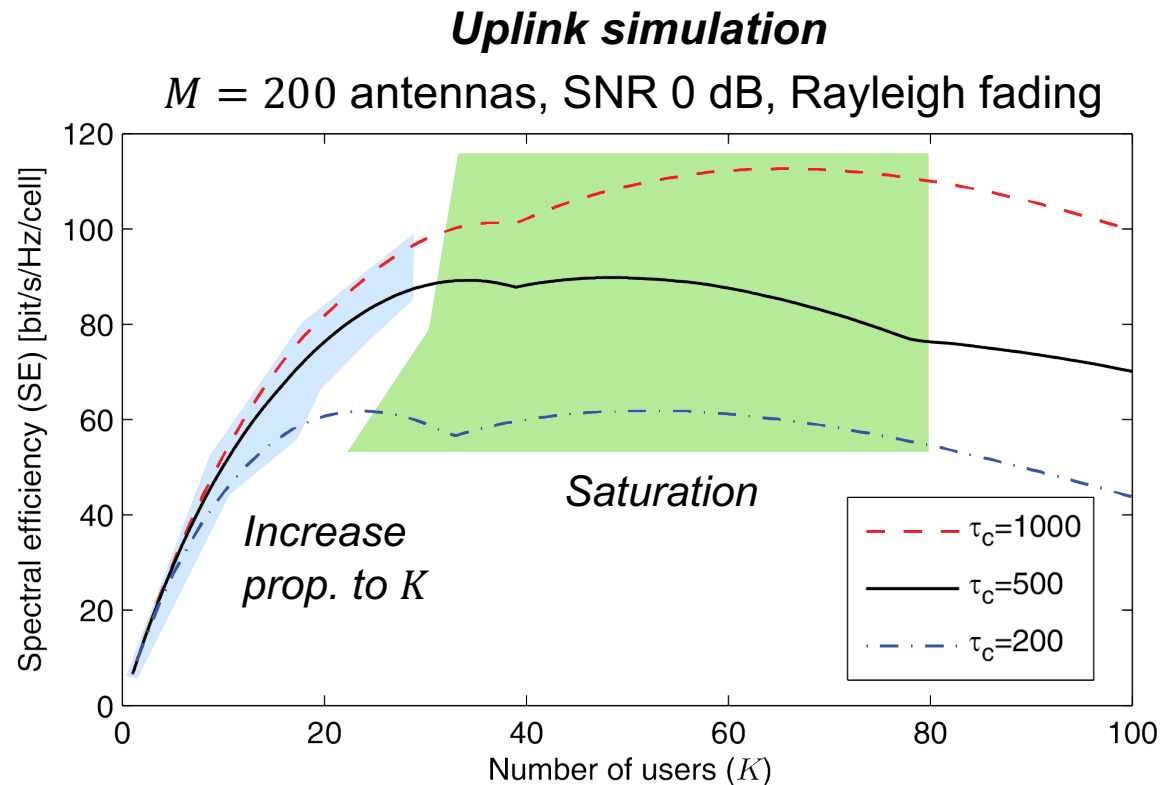
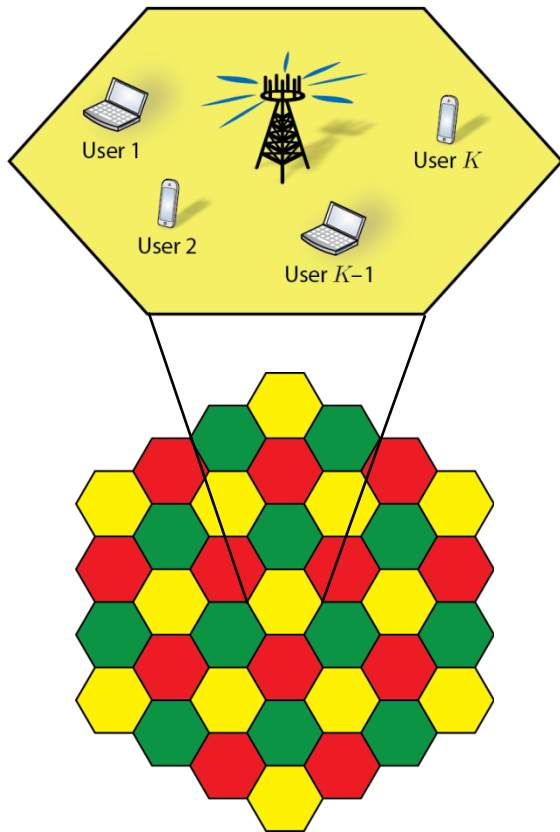


## Key Benefits of Massive MIMO

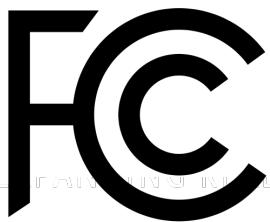
Outdoor users: Handle mobility and guarantee coverage

Indoor users: No need to put BSs inside buildings

# How Much can Spectral Efficiency be Improved?



- *Baseline: 2.25 bit/s/Hz/cell (IMT-Advanced)*
- *Massive MIMO: 25 $\times$ –50 $\times$  improvement*
- Large coherence  $\tau_c$  is key  $\rightarrow$  Use lower frequencies



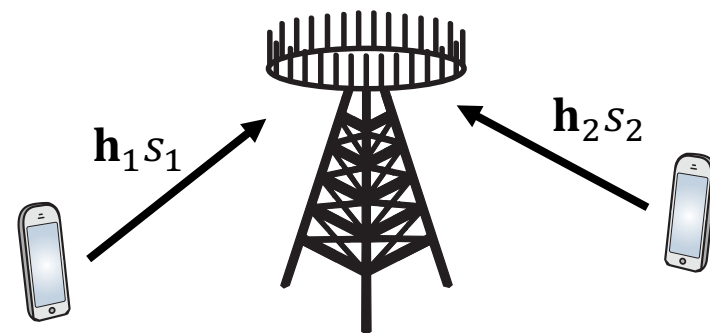
**Yes, FCC's 50 $\times$  goal is within reach!**

# Basic Properties of **MASSIVE MIMO**

# Asymptotic Channel Orthogonality

- Example: Uplink with i.i.d. Rayleigh Fading

- Two users, send signals  $s_k$  for  $k = 1, 2$
- Channels:  $\mathbf{h}_k = [h_{k1} \dots h_{kM}]^T \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_M)$
- Noise:  $\mathbf{n} \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_M)$
- Received:  $\mathbf{y} = \mathbf{h}_1 s_1 + \mathbf{h}_2 s_2 + \mathbf{n}$



- Linear Detector  $\mathbf{w}_1$  for User 1:  $\tilde{y}_1 = \mathbf{w}_1^H \mathbf{y} = \boxed{\mathbf{w}_1^H \mathbf{h}_1} s_1 + \boxed{\mathbf{w}_1^H \mathbf{h}_2} s_2 + \boxed{\mathbf{w}_1^H \mathbf{n}}$
- Maximum ratio filter:  $\mathbf{w}_1 = \frac{1}{M} \mathbf{h}_1$
- Signal remains:  $\mathbf{w}_1^H \mathbf{h}_1 = \frac{1}{M} \|\mathbf{h}_1\|^2 \xrightarrow{M \rightarrow \infty} \mathbb{E}[|h_{11}|^2] = 1$
- Interference vanishes:  $\mathbf{w}_1^H \mathbf{h}_2 = \frac{1}{M} \mathbf{h}_1^H \mathbf{h}_2 \xrightarrow{M \rightarrow \infty} \mathbb{E}[h_{11}^H h_{21}] = 0$
- Noise vanishes:  $\mathbf{w}_1^H \mathbf{n} = \frac{1}{M} \mathbf{h}_1^H \mathbf{n} \xrightarrow{M \rightarrow \infty} \mathbb{E}[h_{11}^H n_1] = 0$

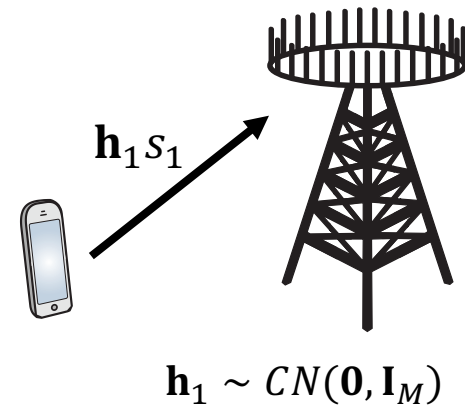
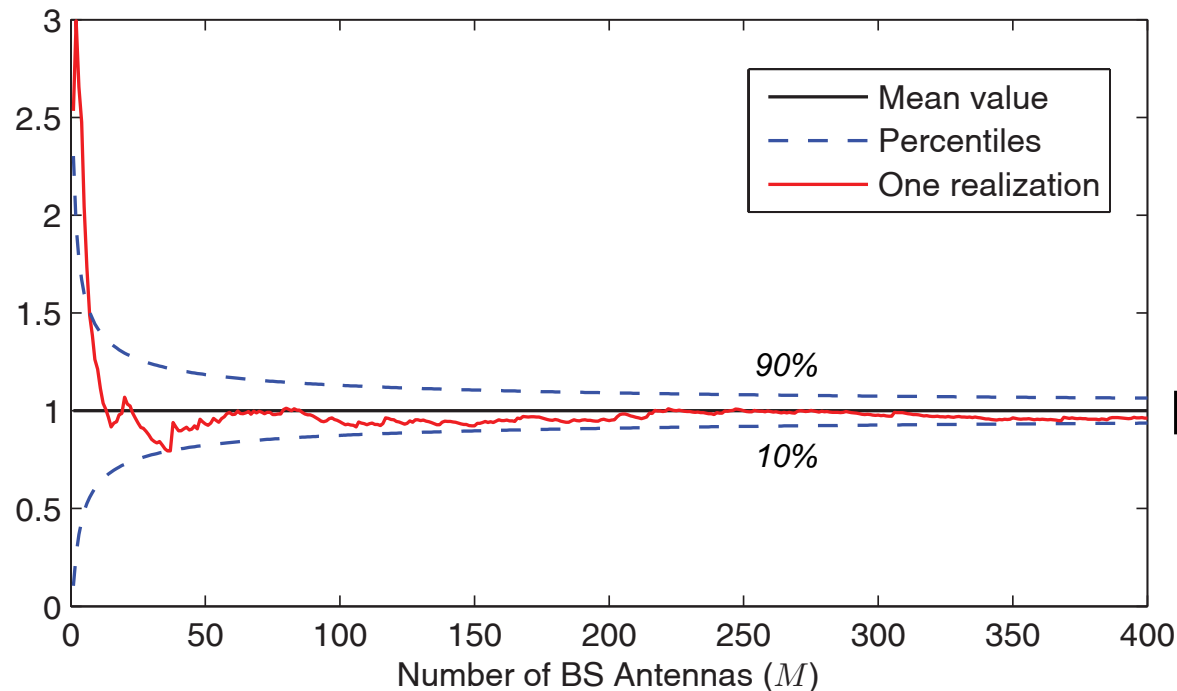
*Asymptotically noise/interference-free communication:  $\tilde{y}_1 \xrightarrow{M \rightarrow \infty} s_1$*



# Asymptotic Channel Hardening

Variations of effective channel reduce with  $M$ :

$$\frac{1}{M} \|\mathbf{h}_1\|^2 \text{ has } \begin{cases} \text{Mean: } 1 \\ \text{Variance: } 1/M \end{cases}$$



$$\|\mathbf{h}_1\|^2 \approx \mathbb{E}\{\|\mathbf{h}_1\|^2\}$$

**Double benefits:**  $\|\mathbf{h}_1\|^2$  scales with  $M$ , variations reduces

# Orthogonality Only in Isotropic Fading?

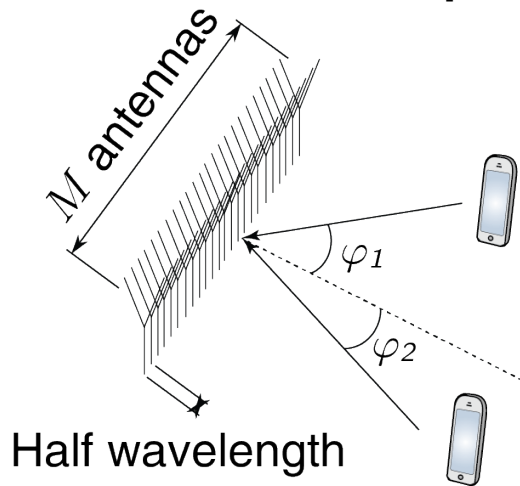
- Assumptions in i.i.d. Rayleigh Fading
  - No dominant directivity
  - Very many scattering objectives

*Less true as  $M \rightarrow \infty$*

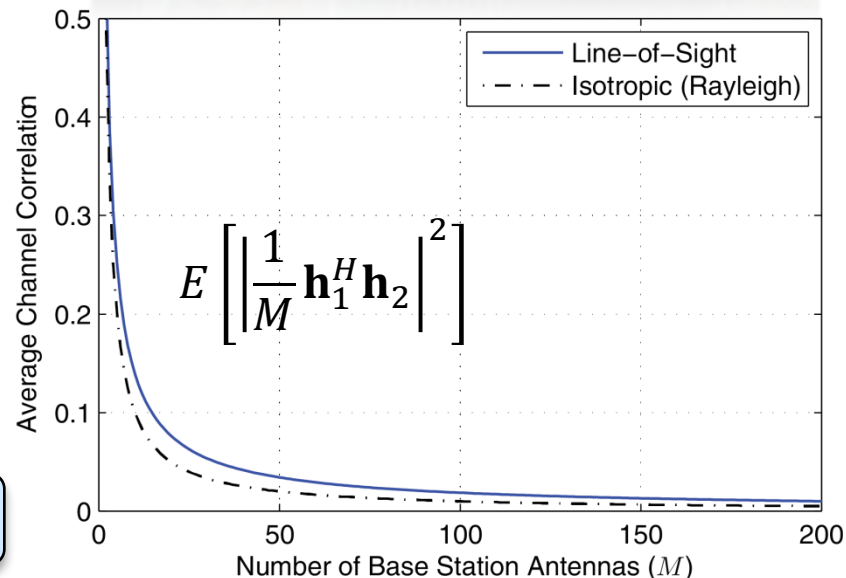


## Example: Line-of-Sight Channels

- Random user angles
- $M$  observations:
  - Stronger signal
  - Suppressed noise
- What is  $\mathbf{h}_1^H \mathbf{h}_2$ ?

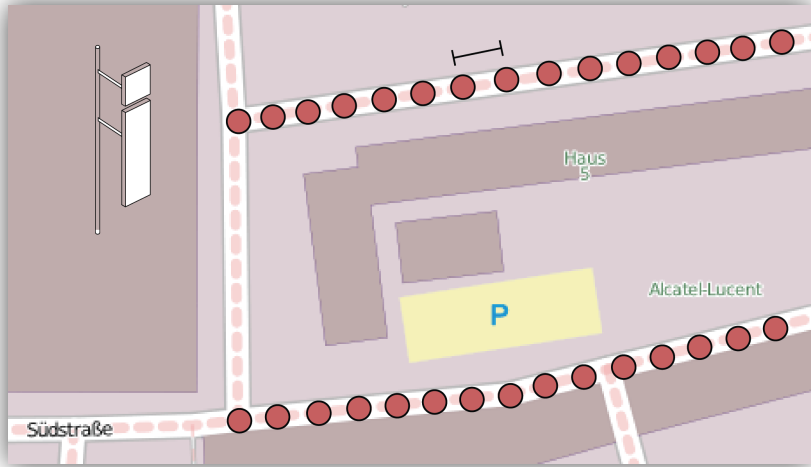


**Difference:** How quickly orthogonality appears

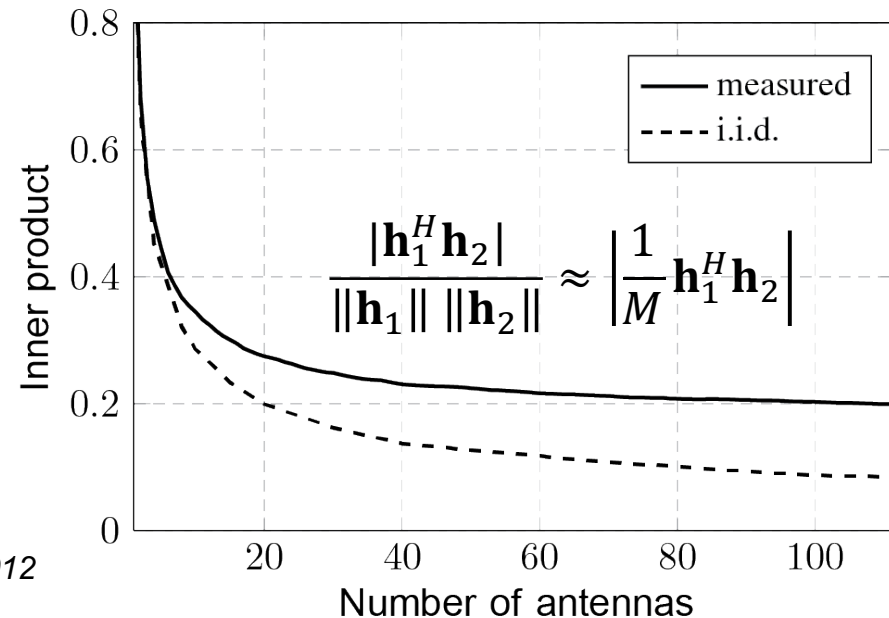


# How Do Practical Channels Behave?

- Measurements show similar results



Source: J. Hoydis, C. Hoek, T. Wild, and S. ten Brink,  
“Channel Measurements for Large Antenna Arrays,” ISWCS 2012

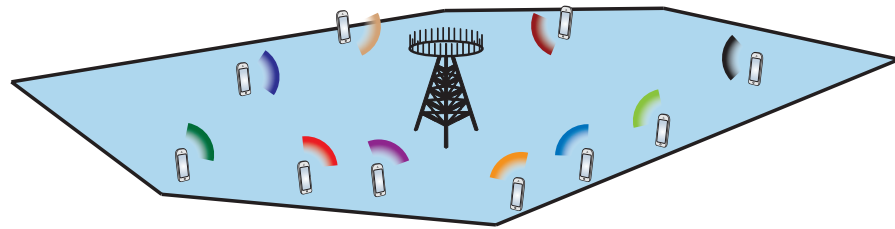


- Asymptotic Favorable Propagation:  $\frac{1}{M} \mathbf{h}_1^H \mathbf{h}_2 \rightarrow 0$  as  $M \rightarrow \infty$ 
  - Achieved in Rayleigh fading and line-of-sight – two extremes!
  - Same behavior expected and observed in practice

Massive MIMO

# TRANSMISSION PROTOCOL

# Classical Multi-User MIMO vs. Massive MIMO



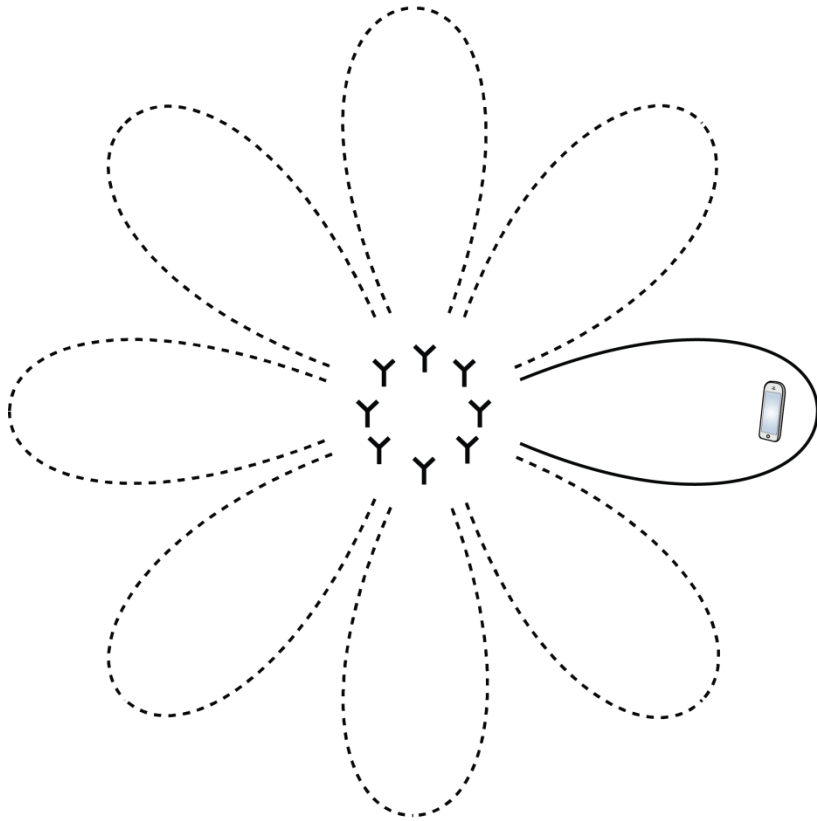
	Classic multi-user MIMO	Massive MIMO (Canonical)
<b>Antennas <math>M</math>, users <math>K</math></b>	$M \approx K$	$M \gg K$
<b>Signal processing</b>	Non-linear is preferred	Linear is near optimal
<b>Duplexing mode</b>	Designed for TDD and FDD	Designed for TDD w. reciprocity
<b>Instantaneous channel</b>	Known at BS and user	Only needed at BS (hardening)
<b>Channel quality</b>	Affected by frequency-selective and fast fading	Almost no channel quality variations (hardening)
<b>Variations in user load</b>	Scheduling needed if $K > M$	Scheduling seldom needed
<b>Resource allocation</b>	Rapid due to fading	Only on a slow time scale
<b>Cell-edge performance</b>	Only good if BSs cooperate	Improved by array gain of $M$
<b>BS cooperation</b>	Highly beneficial if rapid	Only long-term coordination

*FDD = Frequency-division duplex,*

*TDD = Time-division duplex*

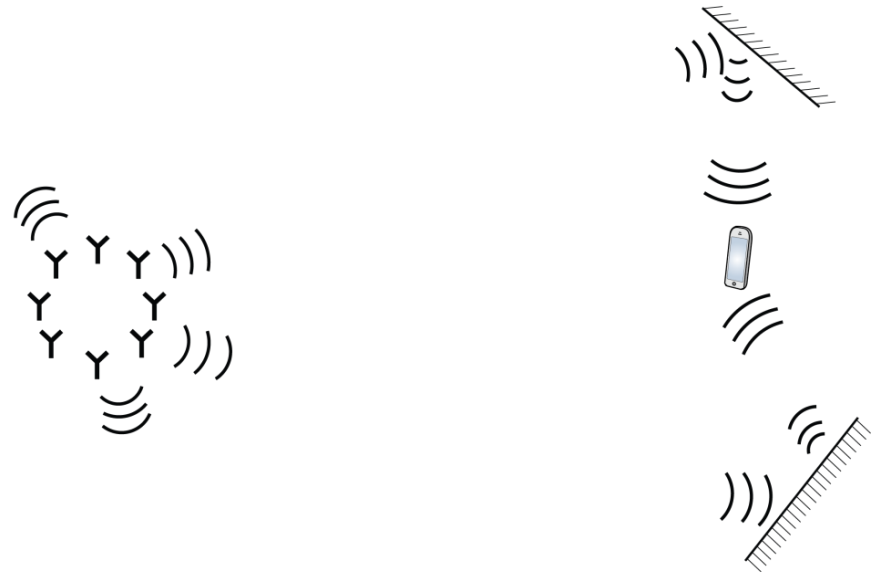
# Downlink MIMO Precoding

*Same principle for MIMO detection*



## **Line-of-Sight**

*Channels characterized by angles*  
*1-2 parameters to estimate per user*  
*Precoding = Angular beamforming*



## **Non-Line-of-Sight**

*Rich multipath propagation*  
 *$M$  parameters to estimate per user*  
*Precoding  $\neq$  Angular beamforming*

**Easy: Codebooks usable (phased array)**

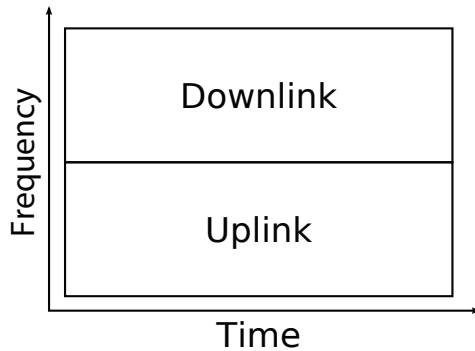
**Hard: Requires pilot transmission!**

# How to Limit the Pilot Overhead?

## Frequency-division duplex (FDD)

Downlink:  $M$  pilots +  $K$  feedback

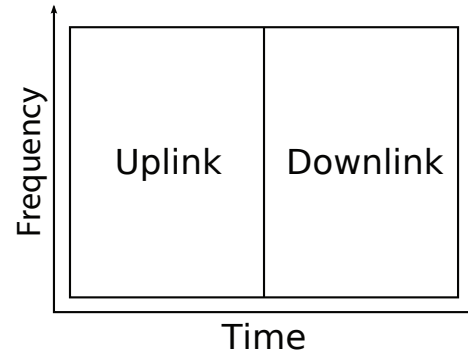
Uplink:  $K$  pilots +  $M$  feedback



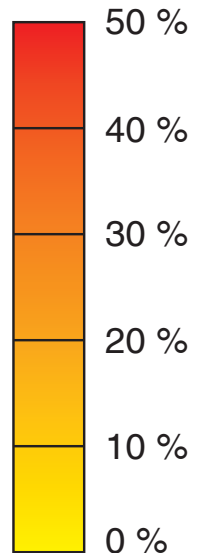
## Time-division duplex (TDD)

Uplink:  $K$  pilots, exploit channel reciprocity

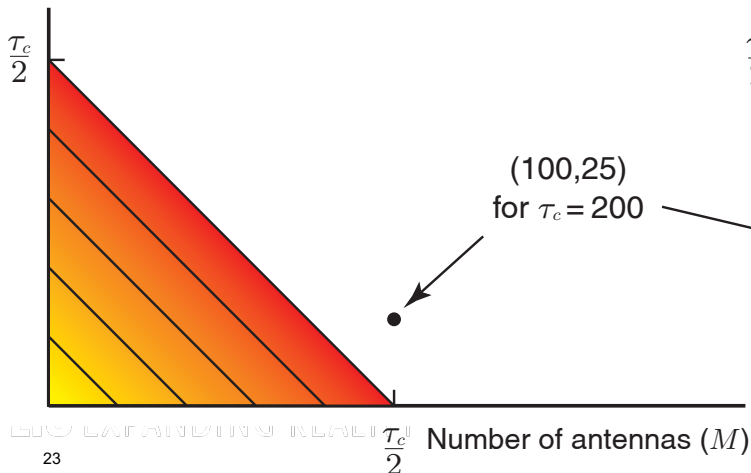
Downlink:  $K$  precoded pilots (optional)



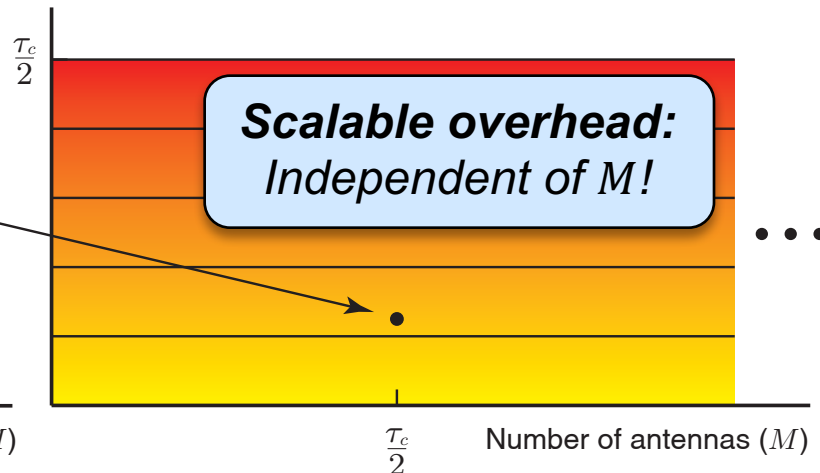
Overhead



Number of users ( $K$ )



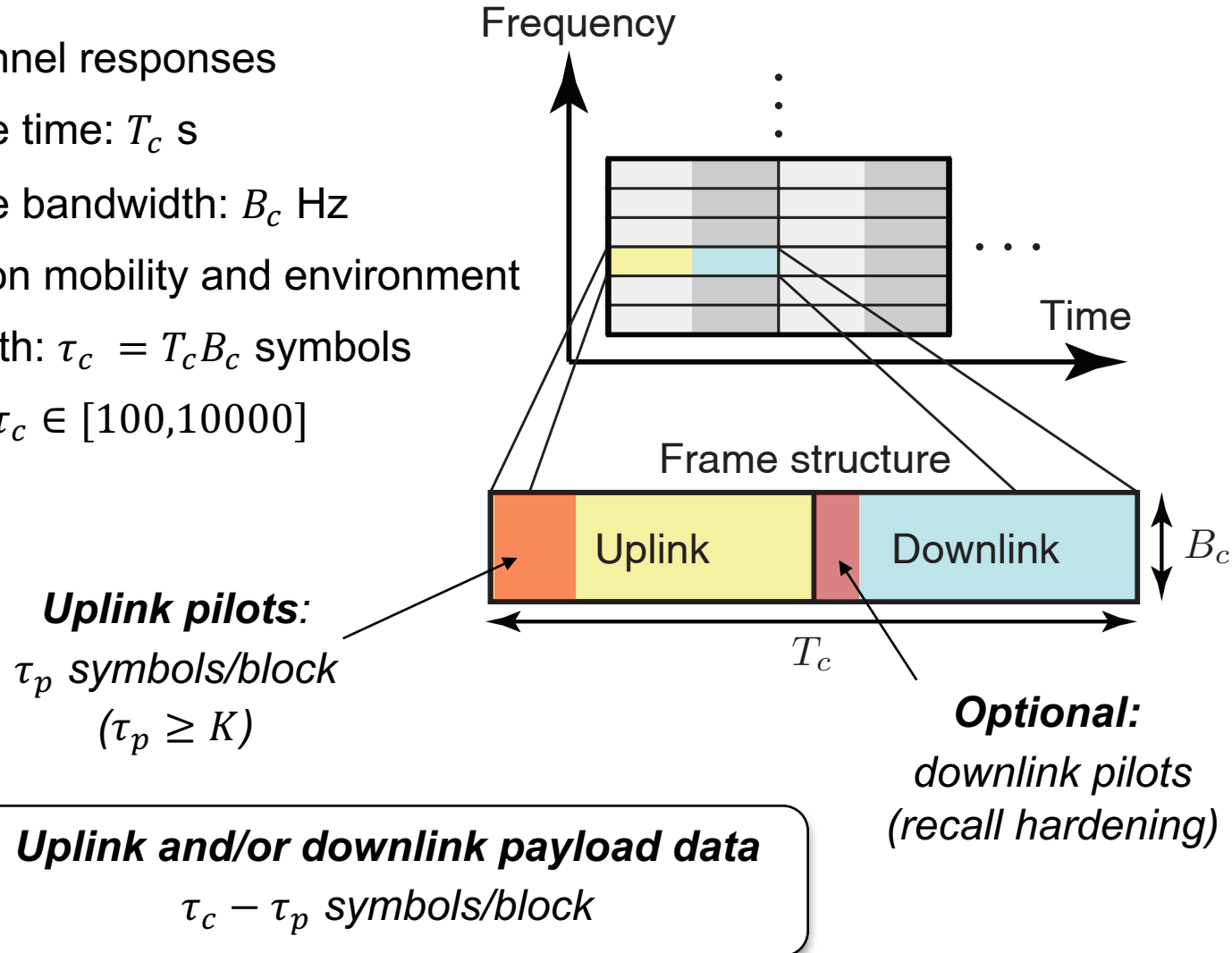
Number of users ( $K$ )



# Massive MIMO TDD Protocol

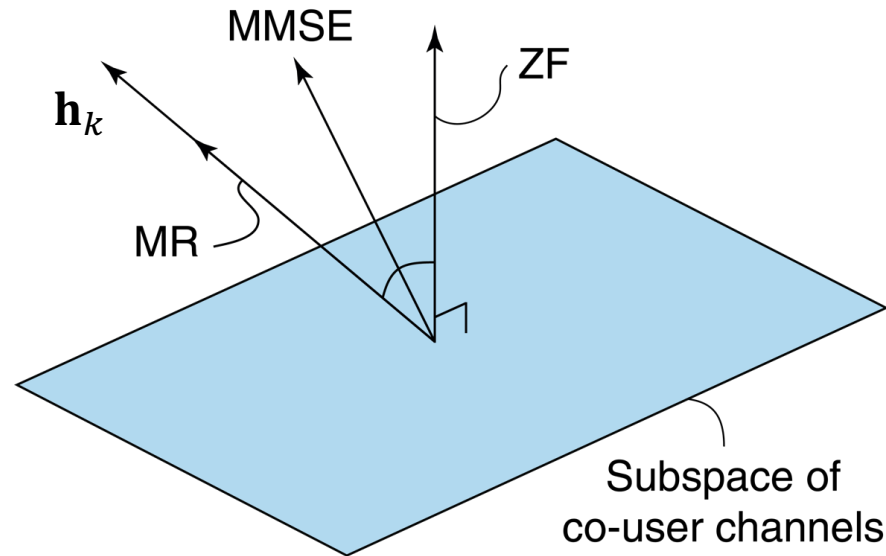
- Coherence Blocks

- Fixed channel responses
- Coherence time:  $T_c$  s
- Coherence bandwidth:  $B_c$  Hz
- Depends on mobility and environment
- Block length:  $\tau_c = T_c B_c$  symbols
- Typically:  $\tau_c \in [100, 10000]$





# Linear Processing Schemes



- Three Options for Downlink Precoding and Uplink Detection
  - Maximum ratio (MR): Maximize received signal power
  - Zero-forcing (ZF): Minimize interference
  - Maximum mean-squared error (MMSE): Balance to signal/interference to minimize uplink MSE

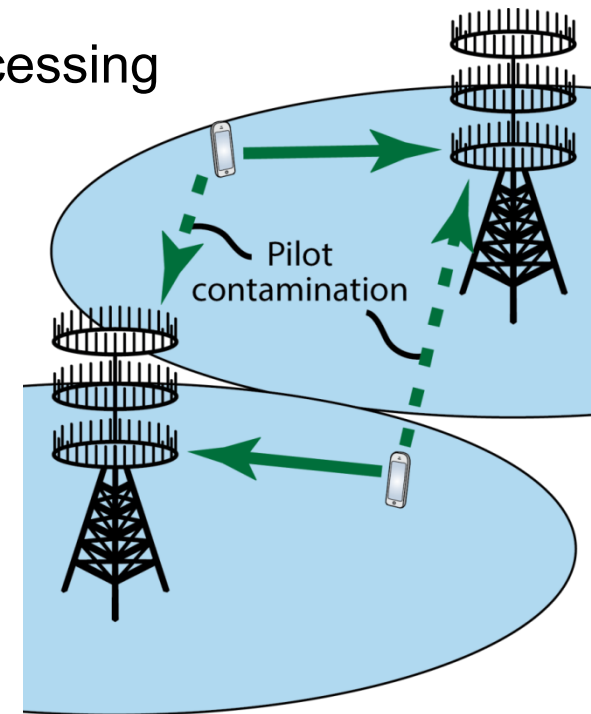
# Channel Acquisition in Massive MIMO

- BS Needs Channel Responses for Linear Processing

- Estimate using  $\tau_p \leq \tau_c$  pilot symbols
- Must reuse pilot sequences in different cells

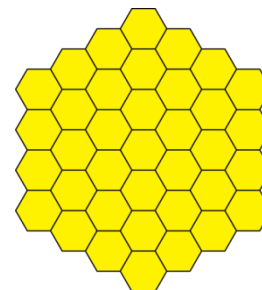
- Called: Pilot Contamination

- BSs cannot tell some users apart
- Recall: Noise and interference vanish as  $M \rightarrow \infty$
- Not interference between users with same pilot!

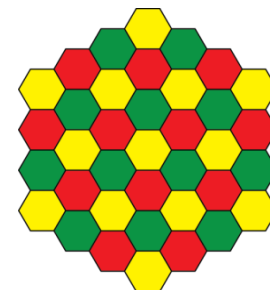


- Scalable Solution: Select how often pilots are reused

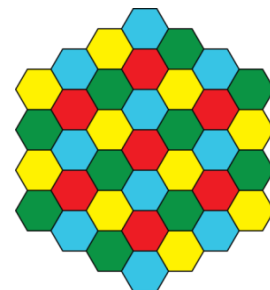
- Pilot reuse factor  $f \geq 1$
- Users per cell:  $K \leq \tau_p/f$
- Higher  $f \rightarrow$  Fewer users per cell, but interferers further away



**Pilot reuse  $f = 1$**



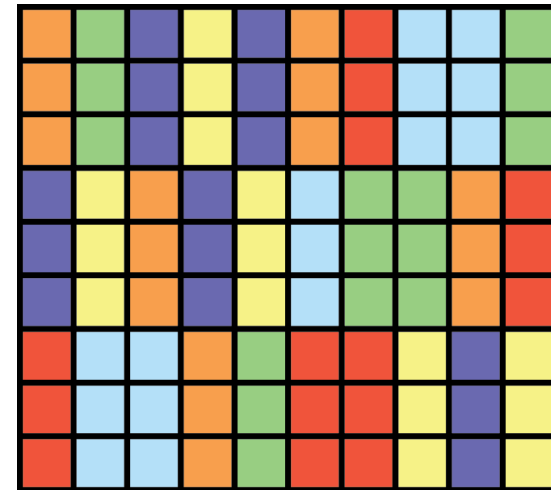
**Pilot reuse  $f = 3$**



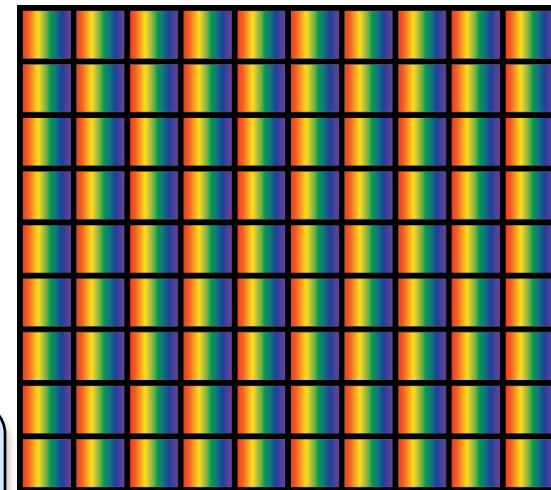
**Pilot reuse  $f = 4$**

# Simple Resource Allocation

- Resource Allocation in 4G
  - Give each time/frequency block to one user
  - Utilize current fading realization
  - *Not needed in Massive MIMO*



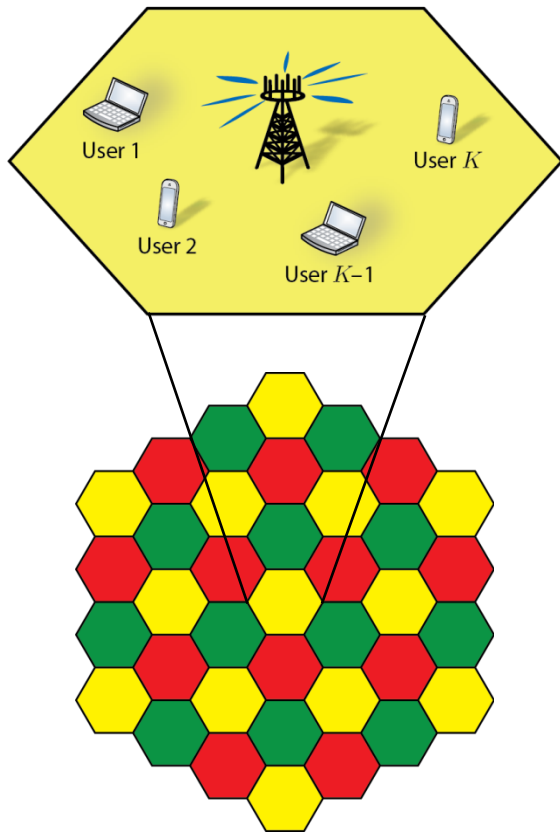
- Spatial Resource Allocation
  - Each user get the whole bandwidth, whenever needed!
  - Separate users spatially
  - Same channel quality in all blocks



***Scalable resource allocation:***

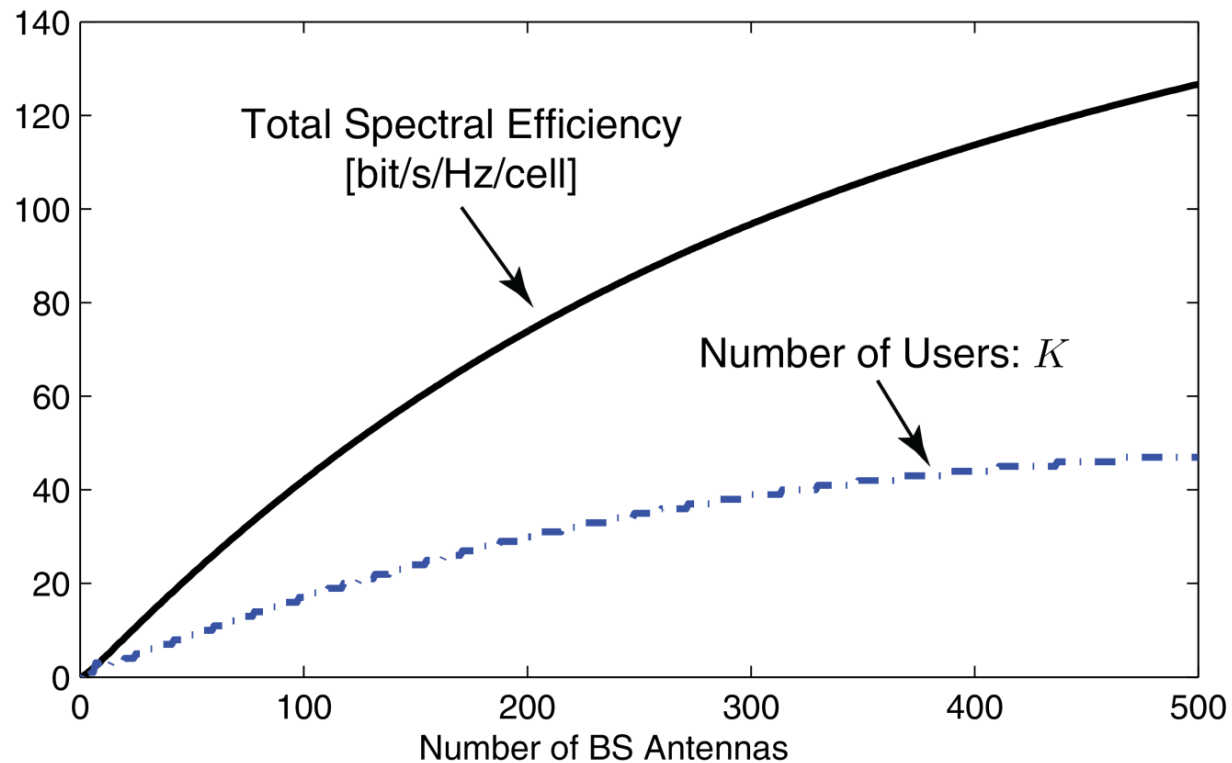
*Only power control based on long-term channel quality*

# How Many Antennas Are Needed?



## ***Uplink simulation***

SNR 5 dB, Rayleigh fading,  
ZF detection,  $\tau_c = 500$ , pilot reuse  $f = 3$

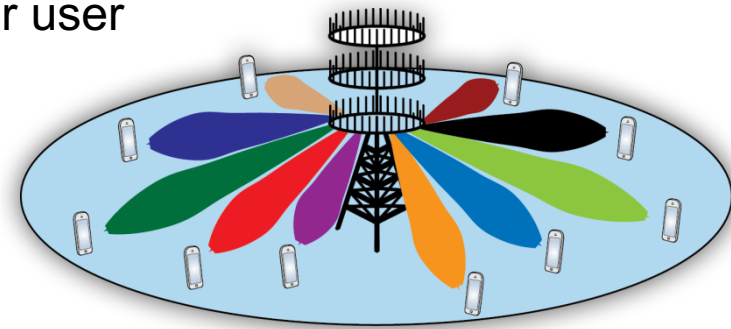


***Massive MIMO is an incredibly scalable technology!***

# SUMMARY

# Summary

- Massive MIMO: The way to increase spectral efficiency in 5G networks
  - >20x gain over IMT-Advanced are foreseen
  - BSs with many small antennas and transceiver chains
  - Higher spectral efficiency per cell, not per user
  - Many potential deployment strategies



- Facts to Remember
  - Massive MIMO  $\neq$  Massive size: TV sized panels at cellular frequencies
  - Favorable propagation in most propagation environments
  - Resource allocation and processing are simplified, not complicated
- Further Reading
  - Emil Björnson, Erik G. Larsson, Thomas L. Marzetta, “*Massive MIMO: 10 Myths and One Critical Question*,” IEEE Commun. Magazine, Feb. 2016.



# Thank you!

Emil Björnson

***Slides and papers available online:***

*<http://www.commsys.isy.liu.se/en/staff/emibj29>*